Example 6.38 Design a low pass filter using rectangular window by taking samples Nov'05 (set 1) of w(n) and with cut-off frequency of 1.2 rad/sec

Solution
$$\omega_C = 1.2 \text{ rad/sec}$$
If $T = 1 \text{ sec}$
The cutoff frequency $\omega_C = 1.2 \text{ rad}$

$$H_d\left(e^{j\omega}\right) = 1 \text{ for } |\omega| < 1.2$$

$$= 0 \text{ for } 1.2 \le |\omega| \le \pi$$

$$h_d\left(n\right) = \frac{1}{2\pi} \int_{-\pi}^{\pi} H_d\left(e^{j\omega}\right) e^{j\omega n} d\omega$$

$$= \frac{1}{2\pi} \int_{-1.2}^{1.2} e^{j\omega n} d\omega$$

$$= \frac{\sin\left(1.2n\right)}{\pi n}$$
For N = 7
$$h_d\left(0\right) = \frac{1.2}{\pi} = 0.387$$

$$h_d\left(-1\right) = h_d\left(1\right) = 0.2967$$

$$h_d\left(-2\right) = h_d\left(2\right) = 0.1075$$

$$h_d\left(-3\right) = h_d\left(3\right) = -0.0469$$

pample 6.41 Design a high pass filter using hamming window with a cutoff frequency of 1.2 radians/sec and N = 9.

Nov'05

Solution

Given $\omega_c = 1.2 \text{ rad/sec}$

The coefficients of high pass filter

$$h_d(0) = 1 - \frac{\omega_C}{\pi} = 0.618$$

$$h_d(n) = \frac{-\sin \omega_C}{\pi n} |n| > 0$$